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*Theory of Superconductivity* is considered one of the best treatments of the field. This monograph, by Nobel Prize-winning physicist J. Robert Schrieffer, has been reprinted because of its enduring value as the introduction to the theory of superconductivity. Based on a series of lectures presented by the author at the University of Pennsylvania, the fundamentals of the microscopic theory of superconductivity are stressed as a means of providing the reader with a framework for the literature in which detailed applications of the microscopic theory are made to specific problems. It also serves as a foundation for the more recent developments in this active field.

The author has developed a number of the formal techniques found in the literature to describe pairing correlations basic to superconductivity. For the most part, only a standard graduate course in quantum theory is required to understand the techniques of quantum mechanics used.

**J. Robert Schrieffer** received his B.S. from MIT. He continued his studies at the University of Illinois, where along with Professors John Bardeen and Leon Cooper he developed the theory of superconductivity. He continued his work as a fellow at the University of Birmingham and the Niels Bohr Institute in Copenhagen. Following work at the Universities of Chicago and Illinois, Schrieffer won the Nobel Prize in 1972 for his work in superconductivity, sharing the honor with Bardeen and Cooper. He was a professor of physics at the University of California, Santa Barbara, and is currently Eminent Scholar Professor at Florida State University and Chief Scientist of the National High Magnetic Field Laboratory.

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# CONTENTS

Editor's Foreword	vii
Preface	xv
Preface to the Revised Printing	xvii
CHAPTER 1 INTRODUCTION	1
1-1 Simple Experimental Facts	4
1-2 Phenomenological Theories	9
CHAPTER 2 THE PAIRING THEORY OF SUPERCONDUCTIVITY	24
2-1 Physical Nature of the Superconducting State	24
2-2 The One-Pair Problem	28
2-3 Landau's Theory of a Fermi Liquid	34
2-4 The Pairing Approximation	36
2-5 Quasi-Particle Excitations	44
2-6 Linearized Equations of Motion	49
2-7 Concluding Remarks	57



CHAPTER 3	APPLICATIONS OF THE PAIRING THEORY	61
3-1	Justification of the Pairing Hypothesis	61
3-2	Acoustic Attenuation Rate	62
3-3	Nuclear-Spin Relaxation Rate	69
3-4	Electromagnetic Absorption	72
3-5	Physical Origin of the Coherence Factors	74
3-6	Electron Tunneling	78
3-7	Other Applications of the Pairing Theory	87
CHAPTER 4	ELECTRON-ION SYSTEM	89
4-1	The Electron-Ion Hamiltonian	89
4-2	Bare Phonons	92
4-3	Bare Electrons	95
4-4	Bare Electron-Phonon Interaction	98
4-5	The Electron-Phonon Hamiltonian	102
CHAPTER 5	FIELD-THEORETIC METHODS IN THE MANY-BODY PROBLEM	103
5-1	The Schrödinger, Heisenberg, and Interaction Pictures	103
5-2	The Green's Function Approach	105
5-3	The Free Fermi Gas	108
5-4	Spectral Representation of $G(\mathbf{p}, \tau)$	112
5-5	Analytic Properties of $G$	115
5-6	Physical Interpretation of $G(\mathbf{p}, p_0)$	116
5-7	Interpretation of $A(\mathbf{p}, \omega)$	119
5-8	The One-Phonon Green's Function	124
5-9	Perturbation Series	126
CHAPTER 6	ELEMENTARY EXCITATIONS IN NORMAL METALS	137
6-1	The Electron Gas with Coulomb Interactions	137
6-2	The Coupled Electron-Phonon System	148

CHAPTER 7	FIELD-THEORETIC METHODS APPLIED TO SUPERCONDUCTIVITY	164
7-1	Instability of the Normal Phase	164
7-2	Nambu-Gor'kov Formalism	169
7-3	Zero-Temperature Excitation Spectrum	180
7-4	Extension to Finite Temperature	193
CHAPTER 8	ELECTROMAGNETIC PROPERTIES OF SUPERCONDUCTORS	203
8-1	London Rigidity	203
8-2	Weak-Field Response	206
8-3	The Meissner-Ochsenfeld Effect	212
8-4	Electromagnetic Properties for Finite $q$ and $\omega$	220
8-5	Gauge Invariance	224
8-6	The Vertex Function and Collective Modes	233
8-7	Flux Quantization	240
8-8	The Knight Shift	244
8-9	The Ginsburg-Landau-Gor'kov Theory	248
CONCLUSION		254
APPENDIX	SECOND QUANTIZATION FORMALISM	257
A-1	Occupation-Number Representation	257
A-2	Second Quantization for Bosons	259
A-3	Second Quantization for Fermions	265
APPENDIX	NOBEL LECTURES, 1972	267
	Macroscopic Quantum Phenomena from Pairing in Superconductors	
	J. R. Schrieffer	267
	Microscopic Quantum Interference Effects in the Theory of Superconductivity	
	Leon N. Cooper	279
	Electron-Phonon Interactions and Superconductivity	
	John Bardeen	300

xii    Contents

NOTES AND REFERENCES	317
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INDEX	329
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