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Weinberg's unique talents fill an important gap in the scientific literature by providing another thorough, rigorous, and yet very enjoyable and casy-to-read textbook that is bound to become another classic. Weinberg's gigantic effort in organizing and presenting a huge body of experimental and theoretical achievements in this tapidly growing field is a great contribution to the astroparticle community and to fundamental science—from the beginning graduate student to the most advanced practitioner.⁴ Gabriele Veneziano, CERN, Geneva



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