

FOURTH EDITION

Pharmacokinetic & Pharmacodynamic Data Analysis: Concepts and Applications

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Used by educators, scientists and students as a reference source on pharmacokinetics and pharmacodynamics, the updated Fourth Edition is an expanded, comprehensive and practical guide to design, analysis and interpretation of kinetic and dynamic experiments. This new text provides the expertise necessary to solve a wide range of commonly appearing problems in an easy and pedagogic way. The addition of new Case Studies makes each chapter on basic concepts more useful for teaching of undergraduate courses and could also be used to support graduate courses in PK/PD.

- Over 100 datasets and practical solutions
- New Case Studies help readers apply concepts
- New chapter on Experimental Design
- Packed with ready to use models
- Detailed guidance on professional analyses



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