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Sections marked † are at a higher level of specialization and/or are peripheral topics not required to follow the remainder of the book. They may be skipped at first reading.

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