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1. A new chapter on interest rate derivatives (Chapter 26) has been added. This chapter covers interest rate swaps and allows modeling to be diverse in more depth.
2. A new chapter on models and numerical procedures (Chapter 20). Much of this material is new, but some has been transferred from the chapters on exotic options in the fourth edition.