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- information about how material is used and why it is important
- historical information
- key theorems
- the latest results
- the status of open questions