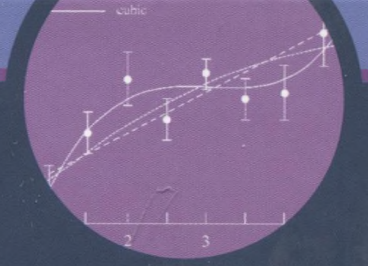
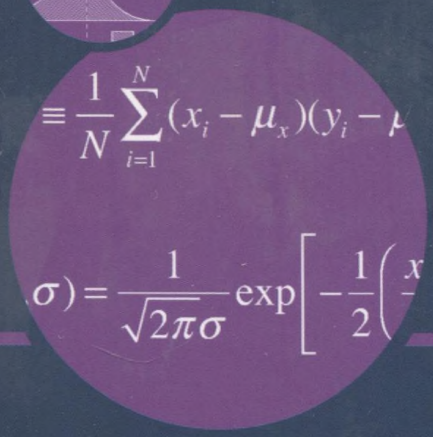




Statistics for Physical Sciences

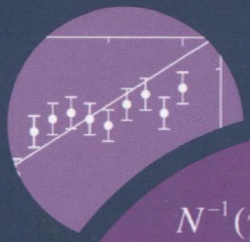
An Introduction

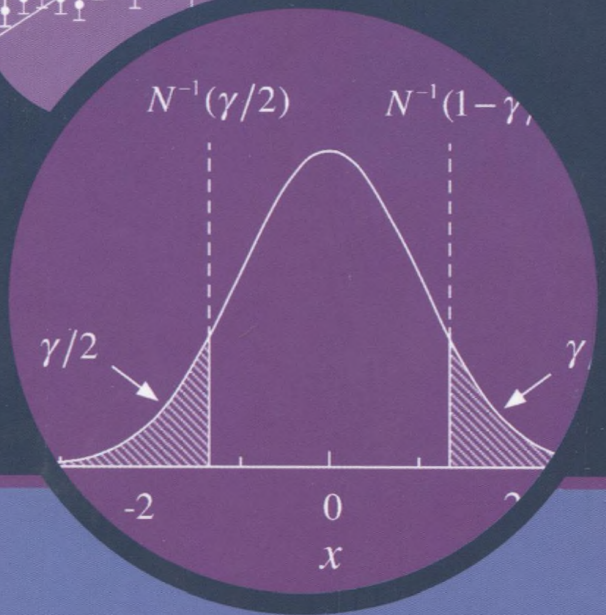
B.R. Martin

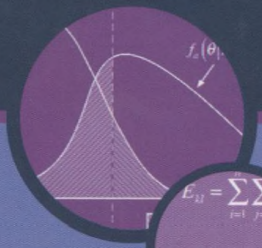
Statistics for Physical Sciences is a short but systematic guide to the ideas and techniques physical scientists encounter in statistical analysis. It combines detailed discussions of a wide range of practical methods with brief descriptions of their theoretical origins, and presents useful formulas and a mathematical account of statistics - all while developing the subject in a logical way.

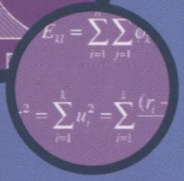
Features

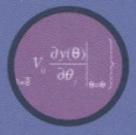
- End of chapter problems encourage understanding of key concepts
- All chapters contain worked examples with real world data
- Detailed discussions focus on statistical methods used specifically in physical sciences











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