

# Contents

|   |           |
|---|-----------|
| Foreword .....  | xvii      |
| Preface .....   | xix       |
| Acknowledgments .....   | xxiii     |
| Authors .....   | xxv       |
| <b>1. Ultra-Realistic Imaging and Its Historical Origin in Display Holography .....</b> | <b>1</b>  |
| 1.1 Ultra-Realistic Imaging and Interferential Techniques .....                         | 1         |
| 1.2 Before Holography .....   | 2         |
| 1.3 Early Holography .....  | 3         |
| 1.4 Display Holography Milestones .....   | 5         |
| 1.4.1 Full-Parallax Transmission Holograms .....  | 6         |
| 1.4.1.1 Earliest Work at Conductron Corporation.....                                    | 6         |
| 1.4.1.2 Early Work in France.....   | 7         |
| 1.4.1.3 Paula Dawson .....  | 8         |
| 1.4.1.4 Nick Phillips and John Webster.....   | 8         |
| 1.4.1.5 John Webster and Margaret Benyon.....   | 10        |
| 1.4.1.6 Ralph Wuerker.....  | 10        |
| 1.4.1.7 40 J Ruby Laser Facility at Fermilab .....                                      | 10        |
| 1.4.1.8 Hologram of Swedish Crown .....   | 11        |
| 1.4.1.9 Carl Fredrik Reuterswärd.....   | 12        |
| 1.4.1.10 Demise of Laser and Mercury Lamp Transmission Holograms .....                  | 14        |
| 1.4.2 Pulsed Holographic Portraits .....  | 14        |
| 1.4.2.1 Use of Neodymium Lasers for Portraiture Applications.....                       | 16        |
| 1.4.2.2 Reagan Portrait and Portraiture into the Future .....                           | 17        |
| 1.4.3 Steven Benton's Rainbow Hologram .....  | 18        |
| 1.4.3.1 Transmission Pseudo-Colour Techniques .....                                     | 18        |
| 1.4.3.2 Large Rainbow Display Holograms and Embossed Holograms .....                    | 19        |
| 1.4.3.3 US Rainbow Displays—Holographics North Inc.....                                 | 20        |
| 1.4.3.4 French Rainbow Displays—AP Holographie SARL .....                               | 20        |
| 1.4.3.5 Australian Rainbow Displays—Australian Holographics Pty. Ltd.....               | 21        |
| 1.4.3.6 Parameswaran Hariharan .....  | 22        |
| 1.4.3.7 Günther Dausmann .....  | 22        |
| 1.4.3.8 Dieter Jung and Rudie Berkhouwt .....   | 22        |
| 1.4.4 Circular Transmission Holograms .....   | 24        |
| 1.4.5 Achromatic or Black-and-White Holograms .....                                     | 24        |
| 1.4.6 Monochrome Reflection Holograms .....   | 26        |
| 1.4.6.1 Sweden—Laserggruppen Holovision AB .....  | 27        |
| 1.4.6.2 Mass Production of Reflection Holograms.....                                    | 30        |
| 1.4.7 Pseudo-Colour Reflection Holograms .....  | 31        |
| 1.4.8 Holographic Movie Films .....   | 33        |
| 1.4.9 Multiplex and Stereographic Holograms .....                                       | 34        |
| 1.5 Digital and Analogue Full-Colour Holography .....                                   | 37        |
| References .....  | 37        |
| <b>2. Lippmann Photography .....</b>  | <b>41</b> |
| 2.1 Brief History of Interferential Colour Recordings .....                             | 41        |
| 2.2 Examples of Interferential Structures in Nature.....                                | 42        |

|           |  |           |
|-----------|--|-----------|
| 2.3       | Lippmann Photography.....  | 43        |
| 2.4       | Theory of the Lippmann Process .....                                   | 46        |
| 2.4.1     | Treatment of Monochromatic Recording.....                              | 46        |
| 2.4.2     | Treatment of Monochromatic Replay .....                                | 46        |
| 2.4.3     | Treatment of Polychromatic Recording.....                              | 47        |
| 2.4.4     | Treatment of Polychromatic Replay.....                                 | 48        |
| 2.5       | Early Lippmann Emulsions .....   | 49        |
| 2.5.1     | Auguste (1862–1954) and Louis Lumière (1864–1948).....                 | 49        |
| 2.5.2     | Richard Neuhauss (1855–1915).....                                      | 50        |
| 2.5.3     | Hans Lehmann (1875–1917) .....   | 51        |
| 2.5.4     | Edmond Rothé (1873–1942).....  | 52        |
| 2.6       | Recording of Early Lippmann Photographs .....                          | 53        |
| 2.6.1     | Recording Equipment .....  | 53        |
| 2.6.2     | Processing Lippmann Silver Halide Emulsions .....                      | 54        |
| 2.6.3     | Viewing Lippmann Photographs .....                                     | 54        |
| 2.6.4     | Early Investigations of Lippmann Emulsions.....                        | 56        |
| 2.6.5     | Museum Collections of Lippmann Photographs .....                       | 57        |
| 2.7       | Modern Lippmann Photography.....                                       | 57        |
| 2.7.1     | Modern Lippmann Emulsions .....  | 58        |
| 2.7.2     | Recording and Processing of Lippmann Photographs Today.....            | 58        |
| 2.7.3     | Modern Lippmann Photographs Made with Different Modern Materials ..... | 58        |
| 2.7.3.1   | Photopolymer Recording Materials .....                                 | 59        |
| 2.7.3.2   | Silver Halide Recording Materials.....                                 | 60        |
| 2.8       | Concluding Remarks.....  | 64        |
|           | References .....   | 65        |
| <b>3.</b> | <b>Continuous Wave Lasers for Colour Holography.....</b>               | <b>71</b> |
| 3.1       | Introduction.....  | 71        |
| 3.2       | Gas Lasers.....  | 72        |
| 3.2.1     | Helium–Neon Laser .....  | 72        |
| 3.2.2     | Argon Ion Laser .....  | 73        |
| 3.2.3     | Krypton Ion Laser.....   | 73        |
| 3.2.4     | Helium–Cadmium Laser .....   | 74        |
| 3.2.5     | Other Gas Lasers.....  | 75        |
| 3.2.5.1   | Helium–Mercury Laser .....   | 75        |
| 3.2.5.2   | Helium–Selenium Laser .....  | 75        |
| 3.2.5.3   | Other Metal Vapour Ion Lasers.....                                     | 75        |
| 3.2.5.4   | Copper and Gold Vapour Lasers .....                                    | 76        |
| 3.3       | Dye Lasers .....   | 76        |
| 3.3.1     | Liquid Dye Lasers .....  | 76        |
| 3.3.2     | Solid-State Dye Lasers.....  | 77        |
| 3.4       | Diode-Pumped Solid-State Lasers.....                                   | 77        |
| 3.4.1     | Green Emission DPSS Lasers.....  | 78        |
| 3.4.1.1   | Verdi 532 nm Laser .....   | 78        |
| 3.4.1.2   | Other Green DPSS Lasers .....  | 78        |
| 3.4.2     | Blue Emission DPSS Lasers .....  | 78        |
| 3.4.3     | Red Emission DPSS Lasers .....   | 80        |
| 3.4.4     | Yellow Emission DPSS Lasers .....                                      | 80        |
| 3.4.5     | Orange Emission DPSS Lasers.....                                       | 80        |
| 3.4.6     | Future DPSS Laser Technology .....                                     | 80        |
| 3.4.6.1   | Praseodymium-Doped Lasers .....  | 80        |
| 3.4.6.2   | Microchip Lasers.....  | 81        |
| 3.4.6.3   | Chromium Forsterite .....  | 81        |

|           |  |           |
|-----------|--|-----------|
| 3.4.6.4   | Optical Parametric Oscillators .....                                   | 81        |
| 3.5       | Semiconductor Diode Lasers .....                                       | 82        |
| 3.5.1     | Introduction.....  | 82        |
| 3.5.2     | Operation and Construction.....  | 82        |
| 3.5.3     | Mode Structure and Coherence .....                                     | 83        |
| 3.5.4     | Operation at Single Longitudinal Mode .....                            | 83        |
| 3.5.5     | Amplification .....  | 84        |
| 3.5.6     | Summary.....   | 85        |
| 3.6       | Fibre Lasers.....  | 85        |
| 3.7       | CW Laser Sources for Colour Holography Today.....                      | 85        |
|           | References .....   | 86        |
| <b>4.</b> | <b>Recording Materials for Colour Holography .....</b>                 | <b>89</b> |
| 4.1       | Introduction.....  | 89        |
| 4.1.1     | Silver Halides .....   | 89        |
| 4.1.2     | Dichromated Gelatin.....   | 90        |
| 4.1.3     | Photopolymers .....  | 90        |
| 4.2       | Holographic Recording .....  | 90        |
| 4.2.1     | Sensitivity of Photographic and Holographic Materials.....             | 93        |
| 4.3       | Holographic Emulsions .....  | 93        |
| 4.3.1     | Demands on Recording Emulsion .....                                    | 93        |
| 4.3.2     | Resolution of Holographic Image .....                                  | 94        |
| 4.3.3     | Image Resolution Determined by Recording Material .....                | 95        |
| 4.4       | Problems due to Short or Long Exposure.....                            | 96        |
| 4.4.1     | Pulsed Holography .....  | 96        |
| 4.4.2     | Reciprocity Failure.....   | 97        |
| 4.4.3     | Holographic Reciprocity Failure.....                                   | 99        |
| 4.5       | Increasing Sensitivity by Hypersensitisation and Latensification ..... | 100       |
| 4.5.1     | Hypersensitisation .....   | 100       |
| 4.5.1.1   | Water Solution of TEA .....  | 100       |
| 4.5.1.2   | Water Treatment .....  | 100       |
| 4.5.2     | Latensification .....  | 100       |
| 4.5.3     | Internal Latensification .....   | 101       |
| 4.6       | Substrates for Holographic Emulsions.....                              | 102       |
| 4.6.1     | Glass Plates .....   | 103       |
| 4.6.2     | Film Substrates .....  | 103       |
| 4.7       | Commercial Recording Materials for Colour Holography .....             | 104       |
| 4.7.1     | Manufacturing Companies .....  | 104       |
| 4.8       | SilverCross Emulsion Research Project .....                            | 105       |
| 4.8.1     | Precipitation Stage .....  | 106       |
| 4.8.2     | Washing Stage .....  | 107       |
| 4.8.3     | Coating Stage .....  | 108       |
| 4.9       | Additional Silver Halide Materials for Holography .....                | 109       |
| 4.10      | DCG Materials.....   | 110       |
| 4.10.1    | Preparing Gelatin Plates .....   | 110       |
| 4.10.2    | Sensitising the DCG Emulsion .....                                     | 110       |
| 4.10.3    | Exposure .....   | 111       |
| 4.10.4    | Pulsed Laser Exposure of DCG .....                                     | 111       |
| 4.10.5    | DCG Processing.....  | 111       |
| 4.10.6    | Panchromatic DCG Emulsions .....                                       | 112       |
| 4.10.7    | Commercial DCG Materials.....  | 115       |
| 4.11      | Photopolymer Materials.....  | 115       |
| 4.11.1    | Recording Photopolymer Holograms with Pulsed Lasers .....              | 116       |

|  |            |
|--|------------|
| 4.11.2 Panchromatic Photopolymers .....  | 117        |
| 4.11.3 Commercial Photopolymer Materials.....  | 118        |
| References .....   | 119        |
| <b>5. Analogue Colour Holography .....</b>   | <b>123</b> |
| 5.1 Introduction.....  | 123        |
| 5.2 Origins in Monochromatic Holography .....  | 124        |
| 5.3 History of True Full-Colour Holography.....  | 126        |
| 5.3.1 Silver Halide-Sensitised Gelatin Technique .....   | 128        |
| 5.3.2 Colour Holograms in Single-Layer Silver Halide Emulsions.....  | 132        |
| 5.4 Colour Recording in Holography.....  | 134        |
| 5.4.1 Colour Theory and Colour Measurements .....  | 134        |
| 5.4.2 Selection of Laser Wavelengths.....  | 137        |
| 5.4.3 Illumination of Colour Holograms .....   | 142        |
| 5.4.4 Demands on Lasers Required .....   | 143        |
| 5.5 Setup for Recording Colour Holograms .....   | 143        |
| 5.5.1 Colour Transmission Holograms .....  | 143        |
| 5.5.2 Colour Reflection Holograms .....  | 143        |
| 5.5.3 Exposure of Colour Holograms .....   | 146        |
| 5.5.4 Processing Recorded Colour Holograms.....  | 148        |
| 5.5.5 Sealing of Colour Holograms .....  | 149        |
| 5.5.6 Recorded and Evaluated Holograms.....  | 150        |
| 5.6 Full-Colour Pulsed Portraiture .....   | 152        |
| References .....   | 153        |
| <b>6. Pulsed Lasers for Holography.....</b>  | <b>157</b> |
| 6.1 Introduction.....  | 157        |
| 6.2 Ruby Laser .....   | 158        |
| 6.2.1 Practical Design of Ruby Lasers Suitable for Holography .....  | 160        |
| 6.2.2 Pulse Lengthening in the Ruby Laser.....   | 161        |
| 6.3 Flashlamp-Pumped Lasers Based on Crystals Doped with Neodymium at 1 $\mu\text{m}$ .....                    | 162        |
| 6.3.1 Nd:YAG .....   | 163        |
| 6.3.2 Nd:YAP and Nd:YLF .....  | 164        |
| 6.3.3 Nd:Glass .....   | 164        |
| 6.3.4 Nd <sup>3+</sup> -Doped Ceramic YAG .....  | 165        |
| 6.3.5 Design of Commercial Neodymium Holography Lasers .....   | 165        |
| 6.3.5.1 Design and Operation of Master Oscillator .....  | 167        |
| 6.3.5.2 Amplification.....   | 167        |
| 6.3.5.3 Pump Electronics.....  | 169        |
| 6.3.5.4 Cooling .....  | 170        |
| 6.3.6 Towards Even Higher Energy .....   | 170        |
| 6.3.7 Applications .....   | 171        |
| 6.4 High-Energy Two-Colour Emission: Stimulated Raman Amplification.....                                       | 172        |
| 6.4.1 SRS Red–Green Pulsed Laser .....   | 173        |
| 6.5 Pulsed RGB Lasers—Neodymium Lasers at 1.3 $\mu\text{m}$ .....  | 176        |
| 6.5.1 Dual-Ring Cavity Pulsed RGB Nd:YLF/Nd:YAG Laser.....   | 177        |
| 6.5.2 Dual Linear-Cavity Pulsed RGB Nd:YAG Laser .....   | 179        |
| 6.5.3 Short-Cavity Pulsed RGB Lasers .....   | 183        |
| 6.5.3.1 Green Lasers.....  | 183        |
| 6.5.3.2 Red and Blue Lasers .....  | 187        |
| 6.5.4 Amplification at 1.3 $\mu\text{m}$ : Higher Energy Emissions in the Red and Blue .....                   | 187        |
| 6.6 Pulsed Holography Lasers Based on Titanium Sapphire (Ti:Al <sub>2</sub> O <sub>3</sub> ) and Cr:LiSAF..... | 187        |
| 6.7 Chromium Forsterite.....   | 189        |

|           |  |            |
|-----------|--|------------|
| 6.7.1     | Injection Seeding .....  | 190        |
| 6.8       | Pulsed Diode-Pumped Lasers for Holography and the Future.....                      | 191        |
|           | References .....   | 193        |
| <b>7.</b> | <b>Digital Colour Holography.....</b>  | <b>197</b> |
| 7.1       | Introduction.....  | 197        |
| 7.2       | Holographic Stereograms .....  | 197        |
| 7.3       | One-Step Digital Holograms .....   | 198        |
| 7.4       | A Simple DWDH Printer.....   | 199        |
| 7.4.1     | Optical Scheme .....   | 199        |
| 7.4.2     | Speckle Blur .....   | 200        |
| 7.4.3     | Operation.....   | 200        |
| 7.4.4     | Image Data .....   | 201        |
| 7.4.5     | Deficiencies .....   | 201        |
| 7.5       | Modern DWDH Printers.....  | 202        |
| 7.5.1     | Use of Pulsed Lasers.....  | 202        |
| 7.5.1.1   | Microsecond Pulsed Lasers.....   | 203        |
| 7.5.2     | Lens-Based Printers .....  | 203        |
| 7.5.3     | Speckle in Lens-Based Printers .....   | 205        |
| 7.5.4     | Triple-Beam Printers.....  | 205        |
| 7.5.4.1   | Hogel-Writing Sequence .....   | 205        |
| 7.5.4.2   | Basic Systems in RGB-Pulsed Laser Triple-Beam Printers.....                        | 206        |
| 7.5.5     | Printers Based on Liquid Crystal on Silicon Displays .....                         | 216        |
| 7.5.6     | Printers Incorporating Variable Reference Beam Systems .....                       | 217        |
| 7.5.7     | HPO Printers.....  | 219        |
| 7.5.8     | Single-Beam RGB Printers.....  | 223        |
| 7.5.8.1   | Screen-Based Hogel Formation Systems .....   | 223        |
| 7.5.9     | Ultra-Realistic Printers .....   | 226        |
| 7.5.9.1   | 3N-Objective Printers .....  | 228        |
| 7.5.10    | DWDH Transmission Hologram Printers.....   | 228        |
| 7.6       | MWDH Printers.....   | 230        |
| 7.7       | Copying Full-Colour DWDH Holograms.....  | 232        |
|           | References .....   | 234        |
| <b>8.</b> | <b>Digital Holographic Printing: Data Preparation, Theory and Algorithms .....</b> | <b>237</b> |
| 8.1       | Introduction.....  | 237        |
| 8.2       | Basic Considerations.....  | 237        |
| 8.3       | Coordinate Systems .....   | 238        |
| 8.4       | Coordinate Meshes .....  | 241        |
| 8.5       | Independent Primary Colours.....   | 242        |
| 8.6       | Viewing Plane .....  | 242        |
| 8.7       | Simple Cases.....  | 243        |
| 8.7.1     | Full-Parallax DWDH “Denisyuk” Reflection Hologram .....                            | 243        |
| 8.7.2     | MWDH Master Hologram .....   | 245        |
| 8.8       | Image-Planed DWDH HPO Holograms.....   | 245        |
| 8.8.1     | Printer, Camera and Viewing Window Options .....                                   | 247        |
| 8.8.2     | General Rectangular Viewing Window .....   | 248        |
| 8.8.2.1   | Simple Translating Camera .....  | 248        |
| 8.8.3     | Centred Camera Configuration .....   | 256        |
| 8.8.4     | Centred SLM Configuration .....  | 260        |
| 8.8.5     | Fundamental Integer Constraints.....   | 263        |
| 8.9       | Rainbow and Achromatic Transmission Holograms.....                                 | 268        |
| 8.9.1     | MWDH .....   | 268        |

|            |  |            |
|------------|--|------------|
| 8.9.1.1    | Vertically Aligned RGB H <sub>1</sub> Master .....   | 268        |
| 8.9.1.2    | Component-Colour H <sub>1</sub> Masters .....  | 271        |
| 8.9.1.3    | Achromatically Tilted Component-Colour H <sub>1</sub> Masters.....                           | 275        |
| 8.9.1.4    | Achromatically Tilted RGB H <sub>1</sub> Master .....  | 276        |
| 8.9.2      | MWDH Achromats.....  | 276        |
| 8.9.3      | DWDH .....   | 276        |
| 8.9.3.1    | Synthesis of the Vertical Slit .....   | 277        |
| 8.9.3.2    | Transformations Required When Using an RGB Laser.....  | 278        |
| 8.9.3.3    | Transformations for One-Colour Laser .....   | 281        |
| 8.10       | Correcting for Inherent Distortion in Printer Optical Objectives .....                       | 283        |
| 8.10.1     | Setting up the Formalism.....  | 283        |
| 8.10.2     | Data Predistortion .....   | 285        |
| 8.10.3     | Non-Paraxial I-to-S Transformations .....  | 288        |
|            | References .....   | 292        |
| <b>9.</b>  | <b>Digital Holographic Printing: Computational Methods for Full-Parallax Holograms .....</b> | <b>293</b> |
| 9.1        | Introduction.....  | 293        |
| 9.2        | Practical Strategies for Changing the Image Plane .....                                      | 294        |
| 9.2.1      | Camera Definition.....   | 295        |
| 9.2.2      | Changing the Image Plane—Two-Step I-to-S Transformations.....                                | 296        |
| 9.2.3      | General Full-Parallax Paraxial Objective Transformations .....                               | 298        |
| 9.2.4      | Non-Paraxial Printer Objectives.....   | 300        |
| 9.2.5      | Larger Holograms .....   | 300        |
| 9.2.6      | Rectangular Viewing Windows .....  | 301        |
| 9.2.6.1    | General Astigmatic Rectangular Viewing Window .....  | 302        |
| 9.3        | Resolution Requirements of DWDH Reflection Holograms .....                                   | 310        |
| 9.4        | DWDH Transmission Holograms .....  | 311        |
| 9.5        | MWDH Reflection Holograms .....  | 312        |
| 9.6        | Full-Parallax and HPO DWDH .....   | 313        |
|            | References .....   | 315        |
| <b>10.</b> | <b>Image Data Creation and Acquisition for Digital Display Holograms .....</b>               | <b>317</b> |
| 10.1       | Introduction.....  | 317        |
| 10.2       | Image Acquisition from a Physical Scene: HPO Holograms .....                                 | 317        |
| 10.2.1     | Simple Translating Camera.....   | 318        |
| 10.2.2     | Hybrid Translating/Rotating Camera with Fixed Target.....                                    | 319        |
| 10.2.3     | Hybrid Translating/Rotating Camera with Optimised Target .....                               | 326        |
| 10.2.4     | Resolution Requirements .....  | 330        |
| 10.2.5     | Image Reduction and Magnification.....   | 331        |
| 10.2.6     | Commercial Holocam Systems.....  | 331        |
| 10.2.7     | Alternative Strategies—Rotating the Object .....   | 334        |
| 10.3       | Image Acquisition from a Physical Scene: Full-Parallax Digital Holograms .....               | 339        |
| 10.3.1     | Horizontal Rotating Platform with Vertically Linear-Translating Camera.....                  | 340        |
| 10.3.1.1   | Calculation of a Centred Camera Data Set .....   | 340        |
| 10.3.1.2   | Derivation of the I-to-S Transformation .....  | 344        |
| 10.3.2     | 3D Structured-Light Scanners .....   | 346        |
| 10.4       | Images Derived from a Virtual Computer Model: HPO Holograms .....                            | 348        |
| 10.4.1     | Data Preparation .....   | 348        |
| 10.4.2     | Creating a 20 cm × 30 cm Landscape Hologram .....  | 349        |
| 10.5       | Images Derived from a Virtual Computer Model: Full-Parallax Holograms .....                  | 357        |
| 10.5.1     | Creating a MAXScript GUI.....  | 357        |
| 10.5.2     | Function of Script .....   | 360        |
| 10.5.3     | Global Variables.....  | 361        |

|            |  |            |
|------------|--|------------|
| 10.5.4     | Writing the “Make Directories” Event Handler .....   | 362        |
| 10.5.5     | Writing the “Calculate” Event Handler .....  | 363        |
| 10.5.6     | Writing the “Make Camera” Event Handler.....   | 364        |
| 10.5.7     | Writing the “Start Render” Event Handler .....   | 365        |
|            | Reference .....  | 368        |
| <b>11.</b> | <b>Theoretical Basis for High-Fidelity Display Holograms .....</b>                           | <b>369</b> |
| 11.1       | Introduction.....  | 369        |
| 11.2       | Three-Dimensional Paraxial Theory of the Thin Transmission Hologram.....                     | 370        |
| 11.2.1     | Collimated Reference and Object Beams.....   | 373        |
| 11.2.2     | Source-Size Blurring .....   | 376        |
| 11.2.3     | Chromatic Blurring.....  | 379        |
| 11.3       | Laser Transmission Holograms and the Problem of Speckle.....                                 | 380        |
| 11.4       | Three-Dimensional Theory of the Thick Transmission Hologram.....                             | 381        |
| 11.4.1     | Snell’s Law at the Air–Hologram Boundary .....   | 382        |
| 11.4.2     | Blurring in the Ultra-Thick Transmission Hologram .....                                      | 383        |
| 11.5       | Reflection Holograms .....   | 384        |
| 11.6       | A Simple Model of the Thick Hologram: Parallel Stacked Mirrors .....                         | 386        |
| 11.7       | Holograms of Finite Thickness.....   | 390        |
| 11.8       | Emulsion Swelling and Change in Refractive Index on Processing.....                          | 393        |
| 11.9       | Non-Paraxial Behaviour and Digital Image Predistortion .....                                 | 394        |
| 11.10      | Solving the Helmholtz Equation in Volume Gratings: Coupled Wave Theory .....                 | 394        |
| 11.10.1    | One-Dimensional Coupled Wave Theory .....  | 394        |
| 11.10.2    | Solution with Perfect Bragg Compliance .....   | 395        |
| 11.10.3    | Boundary Conditions.....   | 397        |
| 11.10.4    | Power Conservation.....  | 398        |
| 11.10.5    | Diffraction Efficiency.....  | 398        |
| 11.10.6    | Small Departure from Bragg Condition.....  | 399        |
| 11.10.6.1  | Behaviour of the Lossless Transmission Hologram.....   | 401        |
| 11.10.6.2  | Behaviour of the Lossless Reflection Hologram.....   | 405        |
| 11.10.7    | Effect of Loss in the Dielectric .....   | 413        |
| 11.10.8    | Recording of Complex Wave Fronts and Multiple Gratings .....                                 | 414        |
| 11.10.9    | Multiple Gratings Generated by Many Object Points .....                                      | 414        |
| 11.10.10   | Recording Multiple Colour Gratings.....  | 418        |
| 11.10.11   | Dispersion Equation Theory .....   | 418        |
| 11.11      | Blurring Revisited.....  | 419        |
| 11.11.1    | Blurring in the Digital Hologram .....   | 420        |
| 11.12      | Computational Methods of Calculating Diffractive Efficiency of Planar Gratings.....          | 421        |
| 11.12.1    | Rigorous Coupled Wave Theory and Rigorous Modal Theory .....                                 | 421        |
| 11.12.2    | Rigorous Chain Matrix Method.....  | 421        |
|            | References .....   | 423        |
| <b>12.</b> | <b>Diffraction Efficiency: An Alternative Approach Using the PSM Model .....</b>             | <b>425</b> |
| 12.1       | Introduction.....  | 425        |
| 12.2       | Formulation of the Simplest Model—The Unslanted Reflection Grating at Normal Incidence ..... | 425        |
| 12.2.1     | Comparison with a Numerical Solution of the Helmholtz Equation.....                          | 429        |
| 12.3       | Unslanted Multiple-Colour Gratings at Normal Incidence .....                                 | 430        |
| 12.3.1     | Numerical Solution for Two-Colour Normal-Incidence Reflection Gratings.....                  | 431        |
| 12.3.2     | Numerical Solution for Three-Colour Normal-Incidence Reflection Gratings.....                | 433        |
| 12.4       | Unslanted Reflection Grating at Oblique Incidence .....                                      | 435        |
| 12.4.1     | $\sigma$ -Polarisation .....   | 435        |
| 12.4.2     | $\pi$ -Polarisation .....  | 438        |

|            |  |            |
|------------|--|------------|
| 12.4.3     | Simplification of PSM Equations to Ordinary Differential Equations.....                                  | 439        |
| 12.4.4     | Analytic Solutions for Sinusoidal Gratings .....   | 440        |
| 12.4.5     | Multiple Colour Gratings.....  | 442        |
| 12.4.6     | Comparison of Kogelnik's Theory with the PSM Theory for Unslanted<br>Gratings at Oblique Incidence ..... | 443        |
| 12.5       | Slanted Reflection Gratings .....  | 445        |
| 12.5.1     | Analytical Solutions for Single-Colour Gratings .....  | 446        |
| 12.6       | Slanted Reflection Gratings in Three Dimensions .....  | 448        |
| 12.7       | Transmission Gratings with Slanted Fringes.....  | 450        |
| 12.8       | Comparison of the PSM Theory with Kogelnik's Theory for Slanted Gratings.....                            | 450        |
| 12.9       | Polychromatic Slanted Reflection Gratings.....   | 451        |
| 12.10      | Extending PSM to Describe Spatially Multiplexed Monochromatic Gratings .....                             | 451        |
| 12.11      | Coupled Wave Theory, PSM and the Rigorous Coupled Wave Theory .....                                      | 455        |
| 12.12      | Lippmann Photography.....  | 456        |
| 12.13      | Discussion .....   | 458        |
|            | References .....   | 459        |
| <b>13.</b> | <b>Illumination of Colour Holograms.....</b>   | <b>461</b> |
| 13.1       | Introduction.....  | 461        |
| 13.1.1     | Chromatic and Source-Size Blurring .....   | 461        |
| 13.1.2     | Geometry Matching.....   | 464        |
| 13.1.3     | Illumination of HPO Holograms .....  | 465        |
| 13.1.4     | Illumination of Large Rainbow and Rainbow-Achromatic Displays .....                                      | 467        |
| 13.2       | Illumination of Holograms by Laser Sources.....  | 467        |
| 13.2.1     | Importance of Wavelength Matching .....  | 469        |
| 13.2.2     | Illumination of Full-Colour Transmission Holograms.....  | 469        |
| 13.2.3     | Gas Lasers.....  | 470        |
| 13.2.4     | Semiconductor Laser Diodes and Solid-State CW Lasers .....   | 470        |
| 13.3       | Non-Laser Light Sources Used for Hologram Illumination.....  | 471        |
| 13.3.1     | Halogen Lights .....   | 472        |
| 13.3.2     | Special Lamps.....   | 473        |
| 13.3.3     | Mercury Lamps.....   | 473        |
| 13.3.4     | Arc Lamps.....   | 473        |
| 13.3.5     | Plasma Lamps .....   | 474        |
| 13.3.6     | LEDs .....   | 475        |
| 13.3.6.1   | Theory of LED Operation .....  | 476        |
| 13.3.6.2   | Blue to Green LEDs: 450 to 530 nm .....  | 478        |
| 13.3.6.3   | Yellow-Green to Red LEDs: 565 to 645 nm.....   | 478        |
| 13.3.6.4   | LEDs and Hologram Illumination—Wavelength Matching .....   | 478        |
| 13.3.6.5   | White Phosphor LEDs.....   | 478        |
| 13.3.6.6   | Multicolour LEDs .....   | 479        |
| 13.3.6.7   | LED Colour Rendering.....  | 479        |
| 13.3.6.8   | Preferred LEDs for Colour Holography .....   | 481        |
| 13.3.6.9   | Lenses for LED Spotlights .....  | 481        |
| 13.3.6.10  | White LED Spotlights .....   | 482        |
| 13.3.6.11  | Special LED Spotlights for Colour Holograms.....   | 483        |
| 13.3.6.12  | LED and Lamp Safety .....  | 485        |
| 13.4       | Exhibition Facilities and Galleries Suitable for Displaying Holograms .....                              | 486        |
| 13.5       | Edge-Lit Holograms .....   | 489        |
| 13.6       | Illumination of Large Displays .....   | 490        |
|            | References .....   | 491        |

|  |     |
|--|-----|
| <b>14. Applications of Ultra-Realistic Holographic Imaging.....</b>                    | 493 |
| 14.1 Introduction.....   | 493 |
| 14.2 Some Scientific Applications of Holographic Imaging .....                         | 493 |
| 14.2.1 Bubble Chamber Holography.....  | 494 |
| 14.2.2 Holographic Microscopy.....   | 496 |
| 14.2.3 Holographic Endoscopy.....  | 497 |
| 14.3 Visual Applications of Full-Colour Holographic Imaging.....                       | 499 |
| 14.3.1 Holographic Copies of Museum Artefacts .....                                    | 499 |
| 14.3.1.1 Virtual Museum Exhibitions .....  | 499 |
| 14.3.1.2 Museum Holography in Greece.....  | 501 |
| 14.3.1.3 Museum Holography in England.....   | 504 |
| 14.3.1.4 Holographic Reproduction of Oil Paintings .....                               | 505 |
| 14.3.2 Digital Display Holograms for Advertising and Product Promotion .....           | 507 |
| 14.3.2.1 Introduction .....  | 507 |
| 14.3.2.2 Key Organisations .....   | 507 |
| 14.3.2.3 Zebra Imaging .....   | 507 |
| 14.3.2.4 XYZ, Geola and Sfera-S .....  | 507 |
| 14.3.3 Digital Display Holograms for Mapping and Architectural Design .....            | 511 |
| 14.3.3.1 Horizontally Mounted Overhead-Illuminated Holograms.....                      | 511 |
| 14.3.4 Digital Holographic Colour Portraits.....                                       | 512 |
| 14.3.5 Digital Art Holograms .....   | 515 |
| 14.3.6 Smaller Full-Colour Holograms .....   | 515 |
| 14.3.7 Holographic Fuel-Effect Electric Fires.....                                     | 517 |
| 14.4 Future Applications.....  | 517 |
| 14.4.1 Holographic Windows and Super-Realistic 3D Static Displays .....                | 517 |
| 14.4.1.1 Creation of Space—High Virtual Volume Displays .....                          | 518 |
| 14.4.1.2 Constraints on Digital Holograms.....   | 518 |
| 14.4.2 Updateable 3D Holographic Displays.....   | 521 |
| 14.4.3 Real-Time 3D Display Technologies Based on Holography.....                      | 522 |
| 14.4.3.1 Simple Autostereoscopic Systems Based on Holographic Screens.....             | 522 |
| 14.4.3.2 Multiprojector Autostereoscopic Systems Based on Holographic Screens.....     | 522 |
| 14.4.4 Future Real-Time True Holographic Displays.....                                 | 523 |
| References .....   | 525 |
| <b>15. Acronyms .....</b>  | 529 |
| <b>Appendix 1: Historical Origins of Display Holography: Spreading Awareness .....</b> | 537 |
| A1.1 Hologram Exhibitions.....   | 537 |
| A1.2 Commercial and Educational Entities Involved in Holography .....                  | 538 |
| A1.2.1 Companies Producing Holograms .....   | 538 |
| A1.2.2 Hologram Galleries.....   | 539 |
| A1.2.3 Holographic Museums .....   | 540 |
| A1.2.4 Educational Institutes.....   | 540 |
| <b>Appendix 2: History of the Geola Organisation .....</b>                             | 541 |
| A2.1 The Beginning .....   | 541 |
| A2.2 First Meeting in Vilnius.....   | 543 |
| A2.3 Incorporation of Geola UAB .....  | 545 |
| A2.4 First Romanian Exhibition of Large-Format Holography.....                         | 547 |
| A2.5 Start of XYZ .....  | 547 |
| A2.6 Panchromatic Film and Sfera-S .....   | 549 |
| A2.7 Vilnius Digital Printer .....   | 550 |
| A2.8 Sale of XYZ .....   | 552 |

|  |     |
|--|-----|
| <b>Appendix 3: Active Cavity Length Stabilisation in Pulsed Neodymium Lasers .....</b>     | 553 |
| A3.1 Introduction.....   | 553 |
| A3.2 Example of Cavity Stabilisation System Using Heated Rear Mirror Holder .....          | 553 |
| A3.3 Active Cavity Length Stabilisation by Piezo Element.....                              | 557 |
| A3.3.1 Statistical Optimisation Algorithm.....   | 558 |
| A3.4 Extension to Other Lasers.....  | 559 |
| References .....   | 559 |
| <b>Appendix 4: Aberration Correction by Image Predistortion in Digital Holograms .....</b> | 561 |
| A4.1 Introduction.....   | 561 |
| A4.2 Mathematical Model .....  | 561 |
| A4.3 Calculation of Optimal Reference Replay Angle .....                                   | 562 |
| A4.4 Compensation for Geometrical Distortion .....   | 564 |
| A4.5 Compensation for Chromatic Aberration .....   | 566 |
| A4.6 Other Corrections .....   | 568 |
| Reference .....  | 568 |
| <b>Appendix 5: MAXScript Holocam Program .....</b>   | 569 |
| <b>Appendix 6: Design Study of Compact RGB LED Hologram Illumination Source .....</b>      | 573 |
| A6.1 Introduction.....   | 573 |
| A6.2 Monochromatic Light Source .....  | 574 |
| A6.3 Polychromatic Light Source.....   | 575 |
| A6.4 Design of the Main Lens Surface .....   | 577 |
| A6.4.1 Monochromatic Light Source .....  | 577 |
| A6.4.2 Mathematical Formulation.....   | 578 |
| A6.4.3 Geometrical Ray Tracing in the Point-Source Approximation .....                     | 580 |
| A6.4.4 Ray Intersection with Target Plane .....  | 581 |
| A6.4.5 Calculation of Power Density Distribution at Target Plane .....                     | 582 |
| A6.4.6 Numerical Solution .....  | 583 |
| A6.4.7 Ray Tracing with Finite Source Size .....   | 583 |
| A6.4.7.1 Method.....   | 584 |
| A6.4.7.2 Spatial Coherence .....   | 585 |
| A6.5 Selected Cases: Computational Results .....   | 586 |
| A6.5.1 Case 1 .....  | 586 |
| A6.5.2 Case 2 .....  | 589 |
| A6.5.3 Case 3 .....  | 591 |
| A6.6 Commercial Design of Nine-Diode Framing Light Source .....                            | 594 |
| A6.7 Additional Considerations .....   | 595 |
| A6.8 Reflective Light-Source .....   | 595 |
| <b>Appendix 7: Bilinear and Bicubic Interpolation.....</b>                                 | 597 |
| A7.1 Introduction.....   | 597 |
| A7.2 Bilinear Interpolation.....   | 597 |
| A7.3 Bicubic Interpolation .....   | 598 |
| <b>Appendix 8: Rigorous Coupled Wave Theory of Simple and Multiplexed Gratings .....</b>   | 601 |
| A8.1 Introduction.....   | 601 |
| A8.2 Derivation of RCW Equations .....   | 601 |
| A8.3 Simplification in the Case of Simple Non-Multiplexed Grating .....                    | 602 |
| A8.4 Derivation of Boundary Conditions.....  | 602 |
| A8.5 Numerical Solution of RCW Equations.....  | 603 |
| A8.5.1 Comparison of Kogelnik's Theory and PSM Theory with RCW Theory.....                 | 604 |

|   |            |
|---|------------|
| A8.5.2 Comparison of N-PSM Theory with RCW Theory.....                        | 604        |
| A8.5.3 Comparison of N-PSM with RCW Theory for Multicolour Gratings.....      | 606        |
| References .....  | 608        |
| <b>Appendix 9: Recent Developments.....</b>                                   | <b>609</b> |
| A9.1 New Equipment, Materials, Techniques and Applications .....              | 609        |
| A9.2 Progress at Zebra Imaging.....   | 610        |
| A9.3 The <i>Queen Elizabeth II</i> Portrait and the Jersey Postage Stamp..... | 612        |
| A9.3.1 Achromatic Portrait of the Queen.....                                  | 612        |
| A9.3.2 Hologram Postage Stamp of the Queen.....                               | 612        |
| A9.4 Lasers for Colour Holography .....                                       | 614        |
| A9.4.1 New Lasers from Cobolt .....   | 614        |
| A9.4.2 New Lasers from Coherent .....   | 614        |
| A9.4.3 New Lasers from Laser Quantum.....                                     | 614        |
| A9.4.4 Progress in RGB Laser Technology at Geola .....                        | 614        |
| A9.5 Progress in Recording Materials and Recording Techniques .....           | 615        |
| A9.5.1 Surface Plasmon Waves .....  | 615        |
| A9.5.2 Anomalously High Pulsed Sensitivity of Photoresist.....                | 616        |
| A9.6 Printers to Record Digital Colour Holograms .....                        | 616        |
| A9.6.1 CGH Composite Reflection Hologram Printer .....                        | 616        |
| A9.6.2 Pioneer's Compact Holographic Printer .....                            | 617        |
| A9.7 3D Display Systems .....   | 618        |
| A9.7.1 HoloVizio from Holografika .....                                       | 618        |
| A9.7.2 SeeReal Technologies' Holographic 3D Display .....                     | 618        |
| A9.8 New Holography Camera from the Hellenic Institute of Holography.....     | 621        |
| A9.9 HoloKit from Liti Holographics .....                                     | 621        |
| References .....  | 622        |
| <b>Index.....</b>   | <b>623</b> |

ensation at the highest level of the authors' collective knowledge and experience in the area of display holography that includes history, theory, practice, and detailed designs of industrial systems. It includes over 500 photographs, diagrams, and design schematics for the recording and production of ultra-realistic holographic images.

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