

Many people around the globe enjoy Sudoku. Laura Taalman and Jason Rosenhouse understand the entertaining aspects of the Sudoku craze and, in this refreshing and delightful book, have analyzed the puzzle from the perspective of mathematics for the first time."

**Maki Kaji, Godfather of Sudoku**

"Rosenhouse and Taalman have magically transformed the 9x9 Sudoku grid into a window through which we can see how mathematicians think and how mathematics really works. It's hard to imagine that any other book could capture the heart of mathematics so thoroughly, accurately, and vividly. After all, solving puzzles, via a mix of established techniques and MacGyver-esque improvisation, is what both mathematics and Sudoku are all about."

**Mike Krebs, Associate Professor of Mathematics, California State University, Los Angeles, and co-author of *Expander Families and Cayley Graphs: A Beginner's Guide***

"In a clear and entertaining style, the authors show how mathematics can improve your understanding of Sudoku. But more importantly, they demonstrate how Sudoku can also improve your understanding of mathematics."

**Arthur Benjamin, Professor of Mathematics, Harvey Mudd College**

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**INTERIOR ART CREDIT**

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