- "... the perfect introduction to the emerging field of spatial data science."
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 University of Chicago; creator of GeoDa software
- "... an excellent blend of key theoretical concepts and applications ... engaging examples, demonstrative code, and laboratory follow-up exercises make this book suitable for both self-learners and traditional academic settings. Highly recommended."
 - Giorgos Mountrakis, State University of New York College of Environmental Science and Forestry

"An excellent course text for students of GIS, spatial statistics, quantitative geography, and ecology . . . Essential reading for beginning students as well as those who wish to refresh their knowledge."

Michael Batty, Centre for Advanced Spatial Analysis, University
 College London

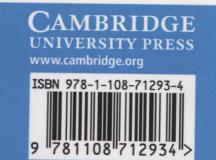
"Highly valuable and timely book for multidisciplinary professionals and students who aim to work with spatial problems . . . an excellent introduction in the concepts and tools to think and analyze spatially."

- Professor Walter T. de Vries, Technical University of Munich

This is an introductory textbook on spatial analysis and spatial statistics through GIS. Each chapter presents methods and metrics, explains how to interpret results, and provides worked examples. The worked examples link theory to practice through a single real-world case study, with software and illustrated guidance. This is a valuable resource for graduate students and researchers analyzing geospatial data through a spatial analysis lens, including those using GIS in the environmental sciences, geography, and social sciences.

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