

### about the book . . .

Investigations by Baire, Lebesgue, Hausdorff, Marczewski, and others have culminated in various schemes for classifying point sets. This important **reference/text** brings together *in a single theoretical framework* the properties common to these classifications.

Providing a clear, thorough overview and analysis of the field, *Point Set Theory* utilizes the axiomatically determined notion of a category base for extending general topological theorems to a higher level of abstraction . . . axiomatically unifies analogies between Baire category and Lebesgue measure . . . enhances understanding of the material with numerous examples and discussions of abstract concepts . . . and more.

Imparting a solid foundation for the modern theory of real functions and associated areas, this authoritative resource is a vital **reference** for set theorists, logicians, analysts, and research mathematicians involved in topology, measure theory, or real analysis. It is an ideal **text** for graduate mathematics students in the above disciplines who have completed undergraduate courses in set theory and real analysis.

### about the author . . .

JOHN C. MORGAN II is Professor of Mathematics at the California State Polytechnic University, Pomona, California. He is the author of numerous research articles concerning topology, measure theory, and real analysis, and a member of the Polish Mathematical Society. Dr. Morgan received the B.A. degree (1964) in mathematics from San Diego State University, California, and M.A. degree (1968) in mathematics and Ph.D. degree (1971) in statistics from the University of California at Berkeley.



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<i>Preface</i>	<i>v</i>
1 Category Bases	1
I Initial Concepts	1
II Singular, Meager, and Abundant Sets	12
III Baire Sets	20
IV Baire Functions	50
2 Point-Meager and Baire Bases	70
I Definitions and Basic Properties	70
II General Properties	74
III Rare Sets	82
IV The Duality Principle	94
3 Separable Bases	102
I Separability	102
4 Cluster Points and Topologies	112
I Cluster Points	112
II Topologies	116
III Topologies Generated by a Topology and an Ideal	119
IV Topological Properties	130



5	Perfect Bases	144
I	Perfect Sets and Bases	144
II	Baire Sets	159
III	Baire Functions	173
6	Translation Bases	192
I	Definitions and Basic Properties	192
II	Arithmetic Operations	198
III	Constructions of Vitali and Hamel	215
IV	Groups and Periodic Functions	230
V	Congruent Sets	244
	<i>Bibliography</i>	251
	<i>Index</i>	276