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*Go forth, my little book! pursue thy way!  
Go forth, and please the gentle and the good.  
William Wordsworth*