

PRAISE FOR
PERPLEXING PARADOXES

“Think you’ve got a fine, analytical mind? Read this book. I can’t tell you how many times I paused and thought, ‘OK, wait a sec... gotta read that again.’ The paradoxes arising out of simple-sounding conditions were, well, mind-boggling. A must-read!”

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“Very paradoxically, paradoxes have had a great influence on the evolution of knowledge. In this book, the master expositor George G. Szpiro narrates the most important ones in his inimitable gripping style, and each is followed by a crystal-clear denouement that explains, in plain English, the resolution. Like a good box of chocolates, it is better to savor each of the chapters individually, either randomly or consecutively, than to fall into the temptation of bingeing all of them at once. Enjoy!”

—**DORON ZEILBERGER**, Board of Governors Professor of
Mathematics, Rutgers University

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—**BARRY CIPRA**, author of
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